

PRZYDATNE WZORY

$$(\cos \alpha + j \sin \alpha)^n = \cos n\alpha + j \sin n\alpha$$

$$\cos(\alpha \pm \beta) = \cos \alpha \cos \beta \mp \sin \alpha \sin \beta$$

$$\sin(\alpha \pm \beta) = \sin \alpha \cos \beta \pm \cos \alpha \sin \beta$$

$$\cos \alpha \cdot \cos \beta = \frac{1}{2}(\cos(\alpha + \beta) + \cos(\alpha - \beta))$$

$$\sin \alpha \cdot \sin \beta = \frac{1}{2}(\cos(\alpha - \beta) - \cos(\alpha + \beta))$$

$$\sin \alpha \cdot \cos \beta = \frac{1}{2}(\sin(\alpha + \beta) + \sin(\alpha - \beta))$$

$$(x^a)' = a \cdot x^{a-1}$$

$$(a^x)' = \ln a \cdot a^x$$

$$(\log_a x)' = \frac{1}{\ln a \cdot x}$$

$$(\sin x)' = \cos x$$

$$(\cos x)' = -\sin x$$

$$(\operatorname{tg} x)' = \frac{1}{\cos^2 x} = \operatorname{tg}^2 x + 1$$

$$(\operatorname{ctg} x)' = -\frac{1}{\sin^2 x} = -\operatorname{ctg}^2 x - 1$$

$$(\operatorname{arc} \sin x)' = \frac{1}{\sqrt{1-x^2}} = -(\operatorname{arc} \cos x)'$$

$$(\operatorname{arc} \operatorname{tg} x)' = \frac{1}{x^2+1} = -(\operatorname{arc} \operatorname{ctg} x)'$$

$$(f \cdot g)' = f' \cdot g + f \cdot g'$$

$$\left(\frac{f}{g}\right)' = \frac{f' \cdot g - f \cdot g'}{g^2}$$

$$(f(g(x)))' = f'(g(x)) \cdot g'(x)$$

$$\int x^a dx = \begin{cases} \frac{x^{a+1}}{a+1} + C, & \text{gd}y \ a \neq -1 \\ \ln|x| + C, & \text{gd}y \ a = -1 \end{cases}$$

$$\int f(g(x)) \cdot g'(x) dx = \int f(u) du, \text{ gdzie } u = g(x)$$

$$\int f(x)g'(x) dx = f(x)g(x) - \int f'(x)g(x) dx$$