

Space curves

- 9.1** Find the tangent plane to the curve $\vec{r} = [a \cos t, b \sin t, e^t]$.
- 9.2** Find the tangent plane to the curve $\vec{r} = [t, t^2, t^3]$ which pass through point $M(2, -\frac{1}{3}, -6)$.
- 9.3** In which points of the curve $\vec{r} = [\frac{a}{2}(1 + \cos u), \frac{a}{2} \sin u, a \sin(\frac{u}{2})]$ tangent plane is parallel to y-axis?
- 9.4** Find equations of normal and binormal lines of the curve $x = y^2, x^2 = z$ at point $P(1, 1, 1)$
- 9.5** Find points of the curve

$$\begin{cases} x = \frac{2}{t} \\ y = \ln t \\ x = -t^2 \end{cases}$$

in which binormal line is parallel to the plane $x - y + 8z + 2 = 0$

- 9.6** Find curvature and torsion of the curves:

- a) $\vec{r} = [u, \frac{1}{2}u^2, \frac{1}{3}u^3]$ dla $u = 1$
- b) $\vec{r} = [e^t, e^{-t}, t\sqrt{2}]$
- c) $\vec{r} = [2t, \ln t, t^2]$