Name $\qquad$

| $\mathrm{CA} . . .$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 1. row | 2. | 3. | 4. | $\sum$ |
|  |  |  |  |  |

1. Write the mathematical formulas corresponding to the following statements with the help of the following signs only: propositional connectives, quantifiers, variables varying through set a) set $\mathbb{N}$ b) $\mathbb{R}$ and symbols indicated in brackets
a) square root of an odd number is odd $(\cdot,+,=, 1)$
b) not every square root of a positive number is positive number $(\cdot,+,=, 1,>, 0)$
2. Prove or disprove $(x, y, z \in \mathbb{R})$
$\exists z \exists x \forall y z \cdot y \neq x$
3. Proof by induction
$14 \mid 3^{4 n+2}+5^{2 n+1}$
4. For how many assignments the formula is true? Transform it into DNF form (e.i. $\left(x_{1} \wedge x_{2} \wedge x_{3}\right) \vee$ $(..) . . \vee(\ldots)$ where $x_{i}$ are variable or their negations)

$$
[(q \vee r) \Rightarrow(r \vee p)] \Rightarrow \sim(p \Rightarrow q)
$$

Name $\qquad$


1. Write the mathematical formulas corresponding to the following statements with the help of the following signs only: propositional connectives, quantifiers, variables varying through a) set $\mathbb{N}$ b) $\mathbb{R}$ and symbols indicated in brackets
a) square root of an even number is even $(\cdot,+,=, 1)$
b) every positive number has a square root $(\cdot,+,=, 1,>, 0)$
2. Prove or disprove $(x, y, z \in \mathbb{R})$
$\exists z \exists x \forall y z \cdot y=x$
3. Proof by induction $9 \mid 4^{n}+15 n+17$
4. For how many assignments the formula is true? Transform it into DNF form (e.i. $\left(x_{1} \wedge x_{2} \wedge x_{3}\right) \vee$ $(..) . . \vee(\ldots)$ where $x_{i}$ are variable or their negations)

$$
[(r \vee q) \Rightarrow(q \vee p)] \Rightarrow \sim(p \Rightarrow r)
$$

