- 1. Write the mathematical formulas corresponding to the following statements with the help of the following signs only: propositional connectives, quantifiers, variables varying through set a) set  $\mathbb{N}$  b)  $\mathbb{R}$  and symbols indicated in brackets
- a) square root of an odd number is  $odd(\cdot, +, =, 1)$
- b) not every square root of a positive number is positive number  $(\cdot, +, =, 1, >, 0)$
- 2. Prove or disprove  $(x, y, z \in \mathbb{R})$

$$\exists z \exists x \forall y \ z \cdot y \neq x$$

3. Proof by induction

$$14|3^{4n+2} + 5^{2n+1}$$

4. For how many assignments the formula is true? Transform it into DNF form (e.i.  $(x_1 \wedge x_2 \wedge x_3) \vee (...) \dots \vee (...)$  where  $x_i$  are variable or their negations)

$$[(q \lor r) \Rightarrow (r \lor p)] \Rightarrow \sim (p \Rightarrow q)$$

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- 1. Write the mathematical formulas corresponding to the following statements with the help of the following signs only: propositional connectives, quantifiers, variables varying through a) set  $\mathbb{N}$  b)  $\mathbb{R}$  and symbols indicated in brackets
- a) square root of an even number is  $even(\cdot, +, =, 1)$
- b) every positive number has a square  $root(\cdot, +, =, 1, >, 0)$
- 2. Prove or disprove  $(x, y, z \in \mathbb{R})$

$$\exists z \exists x \forall y \ z \cdot y = x$$

3. Proof by induction  $9|4^n + 15n + 17$ 

4. For how many assignments the formula is true? Transform it into DNF form (e.i.  $(x_1 \wedge x_2 \wedge x_3) \vee (...) \dots \vee (...)$  where  $x_i$  are variable or their negations)

$$[(r \lor q) \Rightarrow (q \lor p)] \Rightarrow \sim (p \Rightarrow r)$$