Name	
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1. Write the mathematical formulas corresponding to the following statements with the help of the following signs only: propositional connectives, quantifiers, variables varying through set  $\mathbb{N}$  and symbols indicated in brackets

all primes except one are  $\mathit{odd}(\cdot,+,=,1)$ 

2. Prove or disprove  $(x, y, z \in \mathbb{R})$  $\exists x \forall z \forall y \ z \cdot y \neq x$ 

3. Proof by induction that sequence  $a_n = 3^n - 2^n$  is the solution of the recurrence  $a_n = 5a_{n-1} - 6a_{n-2}, a_0 = 0, a_1 = 1.$ 

4. For how many assignments the formula is true? Transform it into DNF form (e.i.  $(x_1 \land x_2 \land x_3) \lor$ (..)...  $\lor$  (...) where  $x_i$  are variable or their negations)

$$[(p \Leftrightarrow q) \Rightarrow r] \Rightarrow [(p \Rightarrow q) \land (q \Rightarrow r)]$$

Name
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1. Write the mathematical formulas corresponding to the following statements with the help of the following signs only: propositional connectives, quantifiers, variables varying through set  $\mathbb{N}$  and symbols indicated in brackets

there is no largest  $\textit{prime}(\cdot,+,=,1)$ 

2. Prove or disprove  $(x, y, z \in \mathbb{R})$ 

 $\forall x \forall y \exists z \ z \cdot y = x$ 

3. Proof by induction that sequence  $a_n = 3^n - 2^n$  is the solution of the recurrence  $a_n = 8a_{n-1} - 15a_{n-2}, a_0 = 0, a_1 = 2.$ 

4. For how many assignments the formula is true? Transform it into DNF form (e.i.  $(x_1 \land x_2 \land x_3) \lor$ (..)...  $\lor$  (...) where  $x_i$  are variable or their negations)

$$[(p \Rightarrow q) \land (q \Rightarrow r)] \Rightarrow [(p \Leftrightarrow q) \Rightarrow r]$$