

Name .....

	HA....	row ....	col....	
1 .	2 .	3 .	4 .	$\Sigma$

1.(2p) Write the mathematical formulas corresponding to the following statements with the help of the following signs only: propositional connectives, quantifiers, variables varying through set  $\mathbb{N}$  and symbols indicated in brackets: *between any two squares there is an even number* ( $\cdot, +, =, <$ )

2.(1p) Proof or disproof. Variables vary through the set  $\mathbb{R}$ .  $\forall x \forall y \exists z x \cdot z = y$ .

3.(2p) Proof by induction

$$\frac{1}{1 \cdot 2} + \frac{1}{2 \cdot 3} + \frac{1}{3 \cdot 4} + \dots + \frac{1}{n(n+1)} = \frac{n}{n+1}$$

4.(3p) Exhibit truth table for the given formula. Transform the formula into DNF form (e.i.  $(x_1 \wedge x_2 \wedge x_3) \vee (\dots) \vee (\dots)$  where  $x_i$  is variable or its negation)

$$[(q \vee \sim r) \Rightarrow (p \wedge \sim r)] \Rightarrow [(\sim q \Rightarrow p) \wedge r]$$

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1.(2p) Write the mathematical formulas corresponding to the following statements with the help of the following signs only: propositional connectives, quantifiers, variables varying through set  $\mathbb{N}$  and symbols indicated in brackets: *between any two even numbers there is an odd number* ( $\cdot, +, =, <, 1$ )

2.(1p) Proof or disproof. Variables vary through the set  $\mathbb{R}$ .  $\forall z \exists y \exists x x \cdot z = y$ .

3.(2p) Proof by induction

$$\frac{1}{1 \cdot 3} + \frac{1}{3 \cdot 5} + \frac{1}{5 \cdot 7} + \dots + \frac{1}{(2n-1)(2n+1)} = \frac{n}{2n+1}$$

4.(3p) Exhibit truth table for the given formula. Transform the formula into DNF form (e.i.  $(x_1 \wedge x_2 \wedge x_3) \vee (\dots) \vee (\dots)$  where  $x_i$  is variable or its negation)

$$[(p \vee \sim r) \Rightarrow (q \wedge \sim r)] \Rightarrow [(\sim p \Rightarrow q) \wedge r]$$