

Name

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1. Write the mathematical formulas corresponding to the following statements with the help of the following signs only: propositional connectives, quantifiers, variables varying through set \mathbb{N} and symbols indicated in brackets

a) *square of an even number is even* ($\cdot, +, =, 1$)

b) *there is no prime number divisible by 6* ($\cdot, +, =, 1, 6$)

2. Proof by induction

$$1^2 - 2^2 + 3^2 - 4^2 + \dots (-1)^{n-1}n^2 = (-1)^{n-1} \frac{n(n+1)}{2}$$

3. Is the following formula a tautology? Transform it into CNF form (e.i. $(x_1 \vee x_2 \vee x_3) \wedge (\dots) \wedge (\dots)$ where x_i are variable or their negations)

$$(p \Leftrightarrow q) \Rightarrow [(\sim p \Rightarrow q) \wedge (p \Rightarrow \sim q)]$$