

Name

| | | row | col.... | |
|----|----|----------|---------|----------|
| 1. | 2. | 3. | 4. | Σ |
| | | | | |

1. Write the mathematical formulas corresponding to the following statements with the help of the following signs only: propositional connectives, quantifiers, variables varying through set a) \mathbb{N} b) \mathbb{Z} and symbols indicated in brackets

a) *a number x has an odd multiple* ($\cdot, +, =, 1$)

b) *every positive number is a square of some number* ($\cdot, +, =, >, 0$)

2. Prove or disprove ($x, y, z \in \mathbb{R}$)

$$\forall y \forall z \exists x \ x \cdot y = z$$

3. Proof by induction

$$11 | 2^{6n+1} + 3^{2n+2},$$

4. Is the following formula a tautology? Transform it into DNF form (e.i. $(x_1 \wedge x_2 \wedge x_3) \vee (\dots) \vee (\dots)$ where x_i are variable or their negations)

$$[(p \vee r) \Rightarrow q] \Rightarrow (p \wedge r)$$

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1. Write the mathematical formulas corresponding to the following statements with the help of the following signs only: propositional connectives, quantifiers, variables varying through set a) \mathbb{N} b) \mathbb{Z} and symbols indicated in brackets

a) *a number x has an even divisor* ($\cdot, +, =, 1$)

b) *every positive number has a square root* ($\cdot, +, =, >, 0$)

2. Prove or disprove ($x, y, z \in \mathbb{R}$)

$$\exists x \forall y \forall z \ x \cdot y = x \cdot z$$

3. Proof by induction $11|2^{6n+1} + 3^{2n+2}$,

4. Is the following formula a tautology? Transform it into DNF form (e.i. $(x_1 \wedge x_2 \wedge x_3) \vee (\dots) \vee (\dots)$ where x_i are variable or their negations)

$$[(p \Rightarrow (q \wedge r)) \Rightarrow r] \Rightarrow (p \wedge r)$$