

NAME:

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Each task is worth 10 points.

1. $V = \{1, 2, \dots, 100\}$, $E = \{\{p, q\} : p, q \in V \text{ and } |p - q| \text{ is a positive even number}\}$, $F = \{\{p, q\} : p, q \in V \text{ and } |p - q| \text{ is an odd number greater than 1}\}$.
 - (a) Is the graph (V, E) connected?
 - (b) Is the graph (V, F) connected?
2. Consider a relation R on \mathbf{R}^2 such that $(a, b)R(c, d)$ iff $bc = ad$.
 - (a) Is R an equivalence relation?
 - (b) If the answer to (a) is YES, find its equivalence classes.
3. Determine whether the following proposition is a tautology: $(\sim q \wedge \sim r) \Rightarrow ((p \vee q) \vee (\sim p \vee r))$.
4. Show that the equation $A \cap (B \div C) = (A \cap B) \div (A \cap C)$ is true for every three sets A, B, C .
5. How many sequences of the length 10, with elements from $\{a, b, c\}$ have exactly four “a” and at least three “b”?
6. How many permutations of the letters: DREAMORTEAM do not have identical consecutive letters?